

Supplementary Trigonometry Exercise Problems

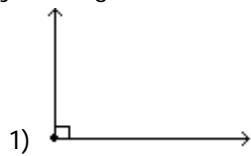
by

Professor Yom

Trig Section 1.1: Angles

MULTIPLE CHOICE.

Classify the angle as acute, right, obtuse, or straight.



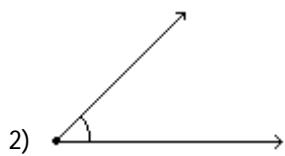
- 1) A) Obtuse

- B) Straight

- C) Acute

- D) Right

1) _____



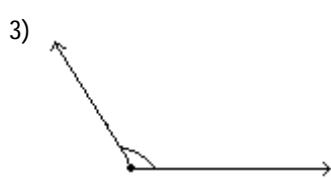
- 2) A) Right

- B) Obtuse

- C) Straight

- D) Acute

2) _____



- 3) A) Right

- B) Obtuse

- C) Straight

- D) Acute

3) _____

4)



- A) Obtuse

- B) Right

- C) Straight

- D) Acute

4) _____

If possible, find the indicated complement or supplement of the given angle.

5) 66° ; supplement

- A) 24°

- B) 204°

- C) 294°

- D) 114°

5) _____

6) 118° ; supplement

- A) 242°

- C) No supplement

- B) 62°

- D) 152°

6) _____

7) 7° ; complement

- A) 83°

- B) 173°

- C) 263°

- D) 353°

7) _____

8) 147° ; complement

- A) 147°

- C) 33°

- B) No complement

- D) 57°

8) _____

SHORT ANSWER.

Find the measure of the indicated angle.

- 9) Two angles of a triangle are 50° and 30° . Find the third angle.

9) _____

- 10) Two angles of a triangle are 40° and 70° . Find the third angle.

10) _____

Answer Key

Testname: MATH 06 - TRIG SECTION 0

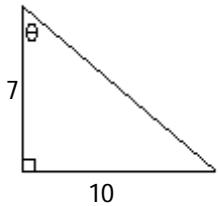
- 1) D
- 2) D
- 3) B
- 4) C
- 5) D
- 6) B
- 7) A
- 8) B
- 9) 100°
- 10) 70°

Trig Section 1.2: The Trigonometric Ratios

MULTIPLE CHOICE.

Find the value of the indicated trigonometric function of the angle θ in the figure. Give an exact answer with a rational denominator.

1)



Find $\csc \theta$.

A) $\csc \theta = \frac{\sqrt{149}}{7}$

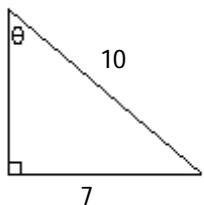
B) $\csc \theta = \frac{7\sqrt{149}}{149}$

C) $\csc \theta = \frac{\sqrt{149}}{10}$

D) $\csc \theta = \frac{10\sqrt{149}}{149}$

1) _____

2)



Find $\cot \theta$.

A) $\frac{10\sqrt{51}}{51}$

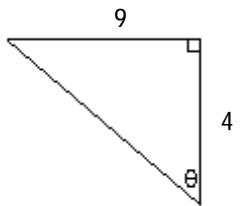
B) $\frac{\sqrt{51}}{10}$

C) $\frac{\sqrt{51}}{7}$

D) $\frac{7\sqrt{51}}{51}$

2) _____

3)



Find $\cot \theta$.

A) $\cot \theta = \frac{9}{4}$

B) $\cot \theta = \frac{4}{9}$

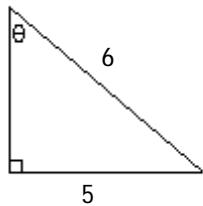
C) $\cot \theta = \frac{4\sqrt{97}}{97}$

D) $\cot \theta = \frac{9\sqrt{97}}{97}$

3) _____

4)

4) _____

Find $\cot \theta$.

A) $\frac{\sqrt{11}}{5}$

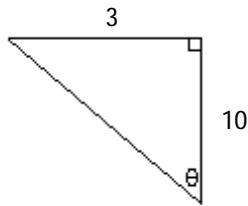
B) $\frac{6\sqrt{11}}{11}$

C) $\frac{5\sqrt{11}}{11}$

D) $\frac{\sqrt{11}}{6}$

5)

5) _____

Find $\tan \theta$.

A) $\tan \theta = \frac{10}{3}$

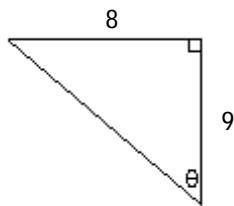
B) $\tan \theta = \frac{\sqrt{109}}{3}$

C) $\tan \theta = \frac{\sqrt{109}}{10}$

D) $\tan \theta = \frac{3}{10}$

6)

6) _____

Find $\tan \theta$.

A) $\tan \theta = \frac{8}{9}$

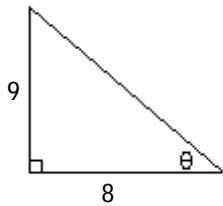
B) $\tan \theta = \frac{\sqrt{145}}{8}$

C) $\tan \theta = \frac{\sqrt{145}}{9}$

D) $\tan \theta = \frac{9}{8}$

7)

7) _____

Find $\cos \theta$.

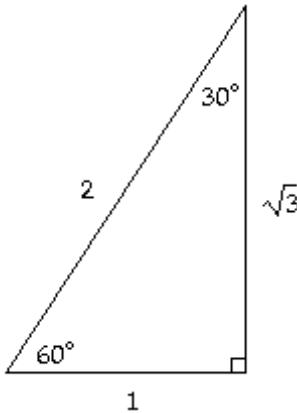
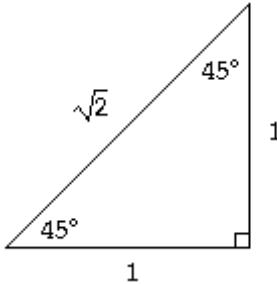
A) $\cos \theta = \frac{\sqrt{145}}{9}$

B) $\cos \theta = \frac{9\sqrt{145}}{145}$

C) $\cos \theta = \frac{8\sqrt{145}}{145}$

D) $\cos \theta = \frac{\sqrt{145}}{8}$

Use the given triangles to evaluate the expression. Rationalize all denominators.



8) $\tan 30^\circ$

A) $\sqrt{3}$

B) $\frac{\sqrt{3}}{3}$

C) $\frac{\sqrt{3}}{2}$

D) 1

8) _____

9) $\csc 60^\circ$

A) 2

B) $\frac{2\sqrt{3}}{3}$

C) $\frac{\sqrt{3}}{2}$

D) $\sqrt{2}$

9) _____

10) $\tan 45^\circ - \sin 60^\circ$

A) $\frac{2\sqrt{3} - 3\sqrt{2}}{6}$

B) $\frac{2 - \sqrt{2}}{2}$

C) $\frac{-\sqrt{3}}{6}$

D) $\frac{2 - \sqrt{3}}{2}$

10) _____

11) $\cot 60^\circ - \cos 45^\circ$

A) $\frac{2\sqrt{2} - 3\sqrt{3}}{6}$

B) $\frac{2\sqrt{3} - 3\sqrt{2}}{6}$

C) $\frac{2 - \sqrt{3}}{2}$

D) $\frac{2 - \sqrt{2}}{2}$

11) _____

12) $\sec 45^\circ$

A) $\sqrt{3}$

B) $\sqrt{2}$

C) $\frac{\sqrt{2}}{2}$

D) $\frac{2\sqrt{3}}{3}$

12) _____

13) $1 - \sin^2 30^\circ - \sin^2 60^\circ$

A) $\frac{1}{4}$

B) $\frac{1 - \sqrt{3}}{2}$

C) 0

D) 1

13) _____

14) $1 + \cot^2 30^\circ - \sec^2 45^\circ$

A) 2

B) 0

C) 1

D) 3

14) _____

SHORT ANSWER.

Use the definition or identities to find the exact value of the indicated trigonometric function of the acute angle θ .

15) $\sec \theta = \frac{13}{12}$ Find $\csc \theta$.

15) _____

16) $\tan \theta = \frac{7}{\sqrt{15}}$ Find $\sin \theta$ and $\cos \theta$.

16) _____

17) $\cos \theta = \frac{2\sqrt{6}}{5}$ Find $\sin \theta$ and $\tan \theta$.

17) _____

18) $\cot \theta = \frac{\sqrt{3}}{3}$ Find $\sin \theta$.

18) _____

Answer Key

Testname: MATH 06 - TRIG SECTION 1

1) C

2) C

3) B

4) A

5) D

6) A

7) C

8) B

9) B

10) D

11) B

12) B

13) C

14) A

15) $\frac{13}{5}$

16) $\sin \theta = \frac{7}{8}$, $\cos \theta = \frac{\sqrt{15}}{8}$

17) $\sin \theta = \frac{1}{5}$, $\tan \theta = \frac{\sqrt{6}}{12}$

18) $\frac{\sqrt{3}}{2}$

Trig Section 1.3: Applying Right Triangles

SHORT ANSWER.

Solve the problem.

- 1) A 29 foot water slide has a 17 foot vertical ladder. How far is it along the ground from the end of the slide back to the base of the ladder that leads to the slide? 1) _____

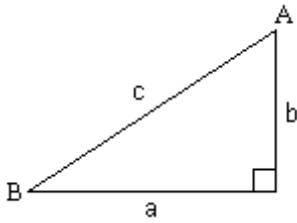
- 2) A painter leans a 30 foot ladder against one wall of a house. At what height does the ladder touch the wall if the foot of the ladder is 10 ft from the base of the wall? 2) _____

- 3) From a distance of 45 feet from the base of a building, the angle of elevation to the top of the building is 68° . Estimate the height of the building to the nearest foot. 3) _____

- 4) A kite is currently flying at an altitude of 15 meters above the ground. If the angle of elevation from the ground to the kite is 35° , find the length of the kite string to the nearest meter. 4) _____

- 5) From a distance of 1217 feet from a spotlight, the angle of elevation to a cloud base is 43° . Find the height of the cloud base to the nearest foot. 5) _____

Solve the right triangle using the information given. Round answers to two decimal places, if necessary.



- 6) $b = 8$, $A = 30^\circ$; Find a , c , and B .

6) _____

- 7) $a = 2$, $A = 40^\circ$; Find b , c , and B .

7) _____

- 8) $a = 7$, $b = 4$; Find c , A , and B .

8) _____

- 9) $a = 4$, $c = 9$; Find b , A , and B .

9) _____

Answer Key

Testname: MATH 06 - TRIG SECTION 2

1) ≈ 23.5 ft

2) ≈ 28.3 ft

3) 111 ft

4) 26 m

5) 1135 ft

6) $a = 4.62$

$c = 9.24$

$B = 60^\circ$

7) $b = 2.38$

$c = 3.11$

$B = 50^\circ$

8) $c = 8.06$

$A = 60.26^\circ$

$B = 29.74^\circ$

9) $b = 8.06$

$A = 26.39^\circ$

$B = 63.61^\circ$

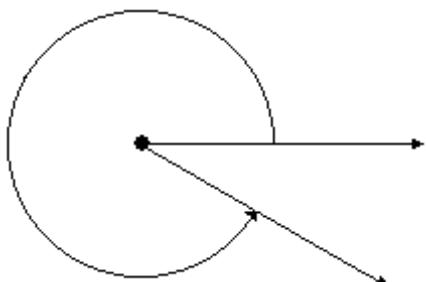
Trig Section 1.4: Trigonometric Functions of Any Angles

MULTIPLE CHOICE.

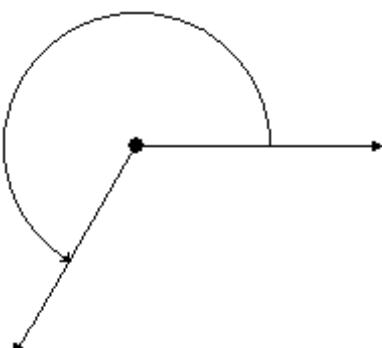
Draw the angle in standard position.

1) 330°

A)

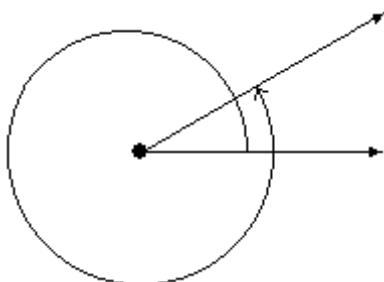


B)

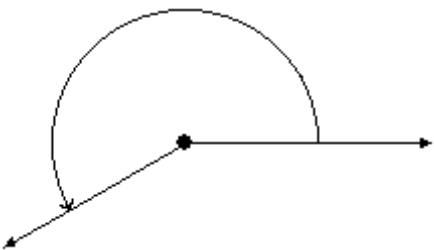


1) _____

C)

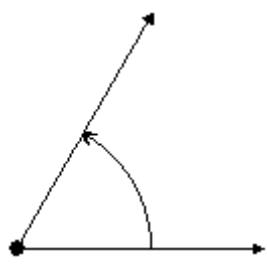


D)

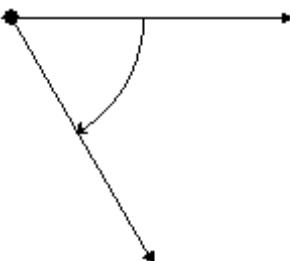


2) 60°

A)

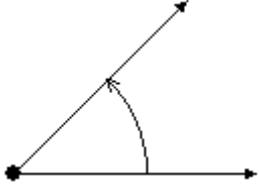


B)

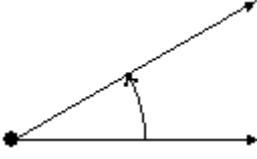


2) _____

C)

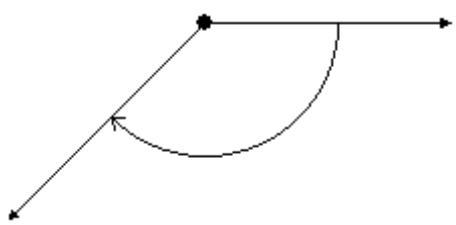


D)

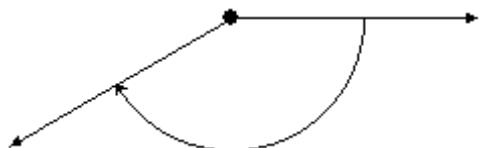


3) -150°

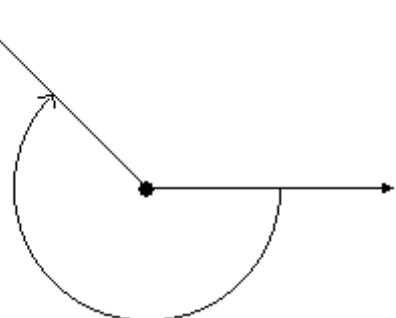
A)



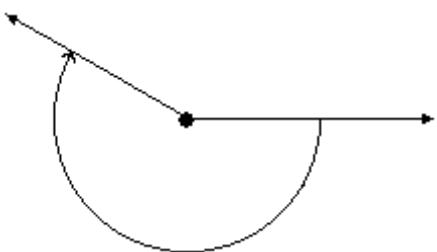
C)



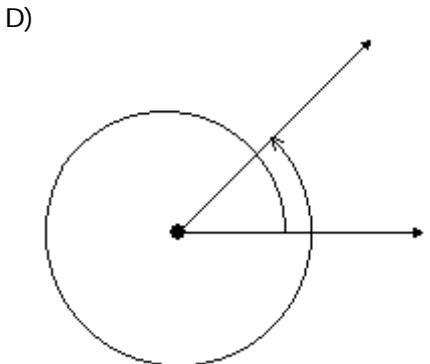
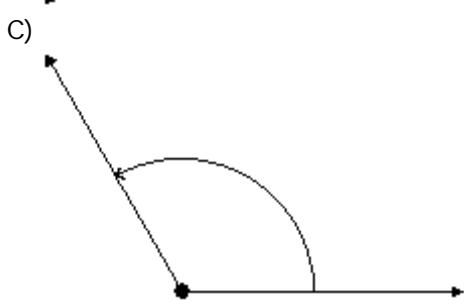
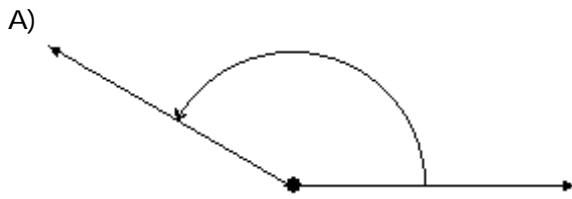
B)



D)



3) _____

4) 405° 

4) _____

Find a positive angle less than 360° that is coterminal with the given angle.5) -185° A) -5° B) 185° C) 355° D) 175°

5) _____

6) 548° A) 274° B) 178° C) 368° D) 188°

6) _____

7) -1031° A) 671° B) 49° C) 311° D) 131°

7) _____

SHORT ANSWER.

Use a coterminal angle to find the exact value of the expression. Do not use a calculator.

8) $\cos 405^\circ$

8) _____

9) $\csc -660^\circ$

9) _____

10) $\cot -180^\circ$

10) _____

MULTIPLE CHOICE.Name the quadrant in which the angle θ lies.

11) $\sin \theta > 0, \cos \theta < 0$

A) I

B) II

C) III

D) IV

11) _____

12) $\tan \theta > 0, \sin \theta < 0$

A) I

B) II

C) III

D) IV

12) _____

13) $\cot \theta < 0, \cos \theta > 0$

A) I

B) II

C) III

D) IV

13) _____

Solve the problem.

14) Which of the following trigonometric values are negative?

14) _____

- I. $\sin(-292^\circ)$
- II. $\tan(-193^\circ)$
- III. $\cos(-207^\circ)$
- IV. $\cot 222^\circ$

A) II, III, and IV

B) III only

C) I and III

D) II and III

SHORT ANSWER.

Find the reference angle of the given angle.

15) 122°

15) _____

16) -42°

16) _____

17) 379°

17) _____

18) -253°

18) _____

19) -517°

19) _____

Use the reference angle to find the exact value of the expression. Do not use a calculator.

20) $\sin 495^\circ$

20) _____

21) $\tan 750^\circ$

21) _____

22) $\cot 390^\circ$

22) _____

Find the exact value of the indicated trigonometric function of θ .

23) $\cos \theta = \frac{2}{9}$, $\tan \theta < 0$ Find $\sin \theta$.

23) _____

24) $\sec \theta = \frac{5}{2}$, θ in quadrant IV Find $\tan \theta$.

24) _____

25) $\tan \theta = -\frac{10}{3}$, θ in quadrant II Find $\cos \theta$.

25) _____

26) $\cot \theta = -\frac{9}{2}$, $\cos \theta < 0$ Find $\csc \theta$.

26) _____

Answer Key

Testname: MATH 06 - TRIG SECTION 3

1) A

2) A

3) C

4) D

5) D

6) D

7) B

8) $\frac{\sqrt{2}}{2}$

9) $\frac{2\sqrt{3}}{3}$

10) undefined

11) B

12) C

13) D

14) D

15) 58°

16) 42°

17) 19°

18) 73°

19) 23°

20) $\frac{\sqrt{2}}{2}$

21) $\frac{\sqrt{3}}{3}$

22) $\sqrt{3}$

23) $-\frac{\sqrt{77}}{9}$

24) $-\frac{\sqrt{21}}{2}$

25) $-\frac{3\sqrt{109}}{109}$

26) $\frac{\sqrt{85}}{2}$

Trig Section 4.1 & 4.2: Radians and Degrees / Arclength

SHORT ANSWER.

Convert the angle in degrees to radians. Express the answer in decimal form, rounded to two decimal places.

1) -139°

1) _____

2) -480°

2) _____

3) 6°

3) _____

4) 12°

4) _____

Convert the angle in radians to degrees. Express the answer in decimal form, rounded to two decimal places.

5) 2

5) _____

6) $\sqrt{2}$

6) _____

Convert the angle in radians to degrees.

7) 3π

7) _____

8) $\frac{\pi}{6}$

8) _____

$$9) \frac{6\pi}{7}$$

$$9) \underline{\hspace{2cm}}$$

$$10) \frac{\pi}{4}$$

$$10) \underline{\hspace{2cm}}$$

Solve the problem.

- 11) The minute hand of a clock is 7 inches long. How far does the tip of the minute hand move in 5 minutes? If necessary, round the answer to two decimal places.

$$11) \underline{\hspace{2cm}}$$

If s denotes the length of the arc of a circle of radius r subtended by a central angle θ , find the missing quantity.

$$12) s = 6.24 \text{ meters}, \theta = 2.6 \text{ radians}, r = ?$$

$$12) \underline{\hspace{2cm}}$$

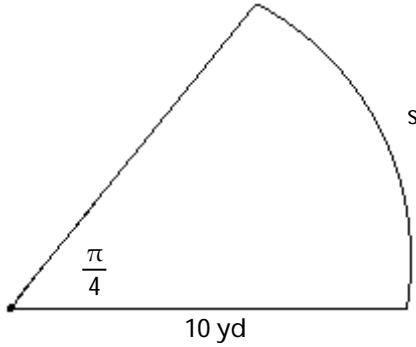
$$13) r = \frac{2}{3} \text{ feet}, s = 14 \text{ feet}, \theta = ?$$

$$13) \underline{\hspace{2cm}}$$

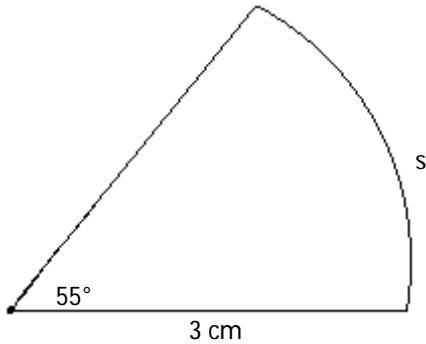
Find the length s . Round the answer to three decimal places.

$$14)$$

$$14) \underline{\hspace{2cm}}$$

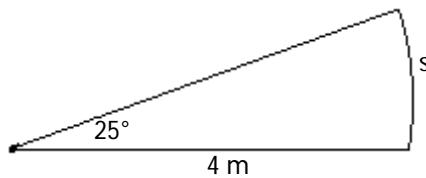


15)



15) _____

16)



16) _____

Solve the problem.

- 17) For a circle of radius 4 feet, find the arc length s subtended by a central angle of 60° . Round 17) _____
to the nearest hundredth.

- 18) A pendulum swings through an angle of 30° each second. If the pendulum is 35 inches long, 18) _____
how far does its tip move each second? If necessary, round the answer to two decimal
places.

Answer Key

Testname: MATH 06 - TRIG SECTION 4&5

- 1) -2.43
- 2) $-\frac{8\pi}{3}$
- 3) $\frac{\pi}{30}$
- 4) 0.21
- 5) 114.59°
- 6) 81.03°
- 7) 540°
- 8) 30°
- 9) 154.29°
- 10) 45°
- 11) 3.67 in.
- 12) 2.4 m
- 13) 21 radians
- 14) 7.854 yd
- 15) 2.88 cm
- 16) 1.745 m
- 17) 4.19 ft
- 18) 18.33 in.

Trig Section 5.1: Graphing the Trigonometric Functions / Unit Circle

MULTIPLE CHOICE.

Solve the problem.

1) What is the domain of the cosine function?

- A) all real numbers, except integral multiples of π (180°)
- B) all real numbers
- C) all real numbers, except odd multiples of $\frac{\pi}{2}$ (90°)
- D) all real numbers from -1 to 1, inclusive

1) _____

2) What is the range of the cosine function?

- A) all real numbers greater than or equal to 0
- B) all real numbers greater than or equal to 1 or less than or equal to -1
- C) all real numbers from -1 to 1, inclusive
- D) all real numbers

2) _____

SHORT ANSWER.

Solve the equation on the interval $0 \leq \theta < 2\pi$.

3) $\cos x = 0$

3) _____

4) $\sin x = -1$

4) _____

5) $\tan x = -1$

5) _____

6) $2 \cos x - \sqrt{3} = 0$

6) _____

7) $2 \sin x + \sqrt{2} = 0$

7) _____

8) $2 \sin x - 1 = 0$

8) _____

9) $\cos \theta - 1 = 0$

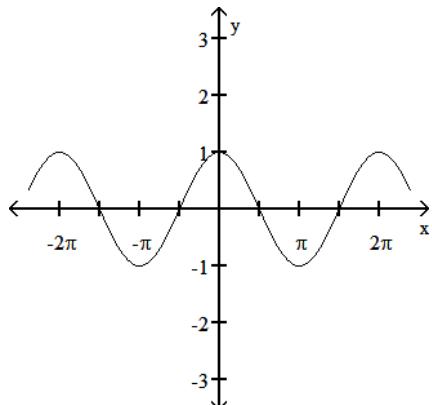
9) _____

MULTIPLE CHOICE.

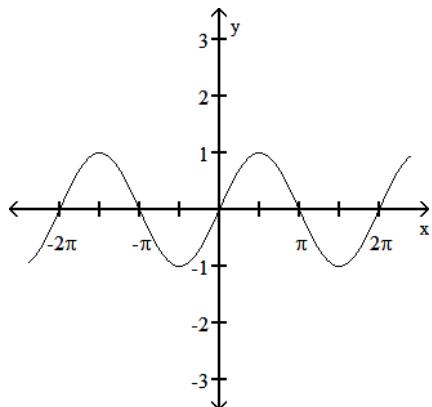
Match the function with its graph.

10) $y = \sin x$

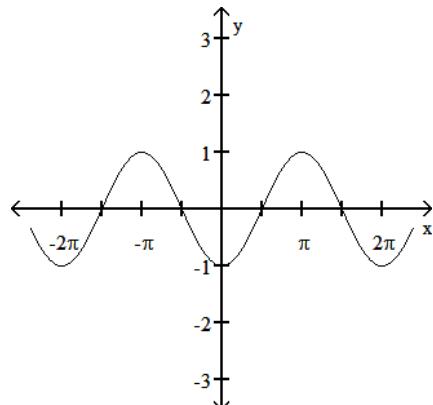
A)



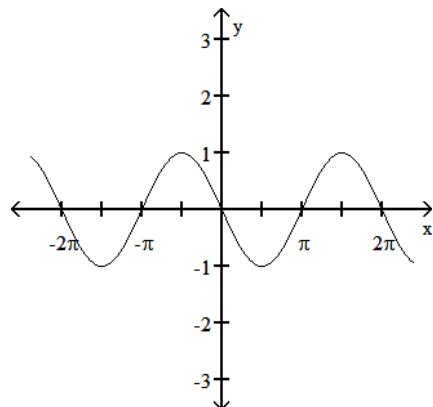
C)



B)



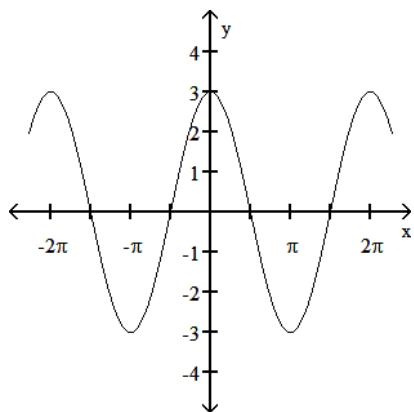
D)



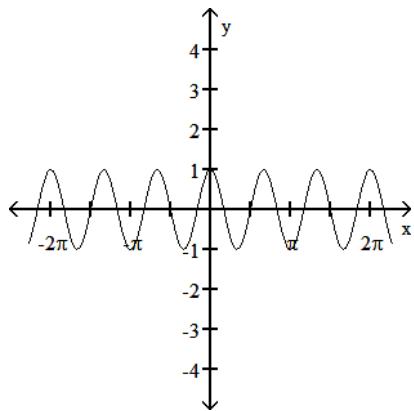
10) _____

11) $y = 3 \sin x$

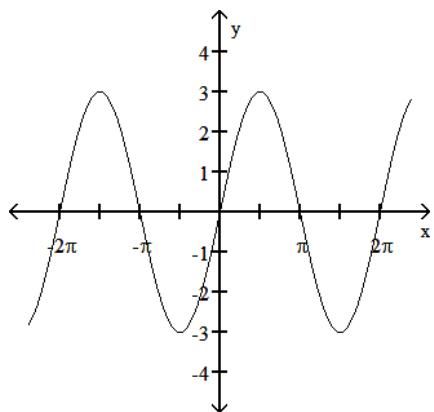
A)



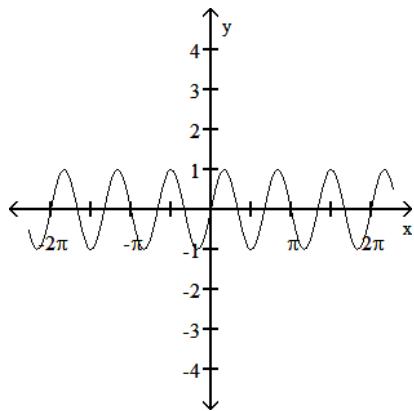
C)



B)



D)

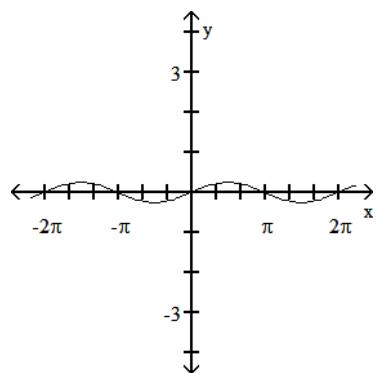


11) _____

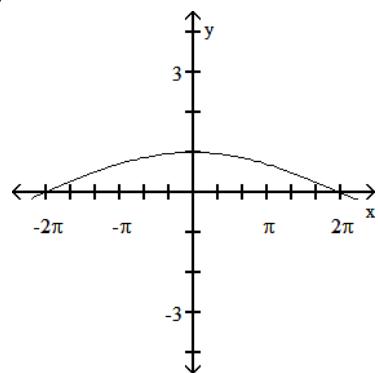
$$12) y = \frac{1}{4} \sin x$$

12) _____

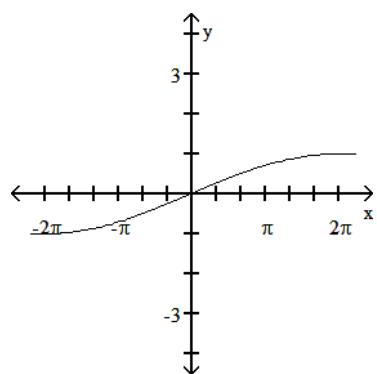
A)



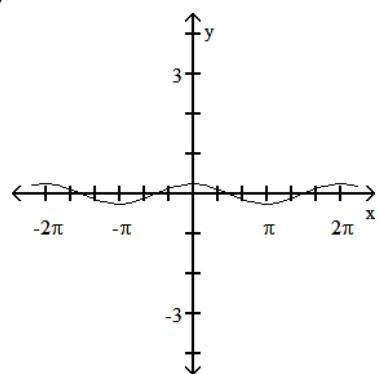
B)



C)

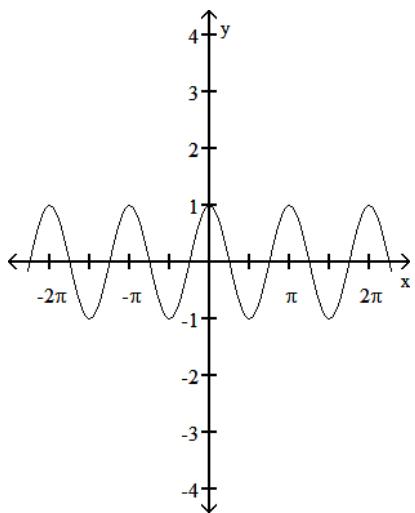


D)

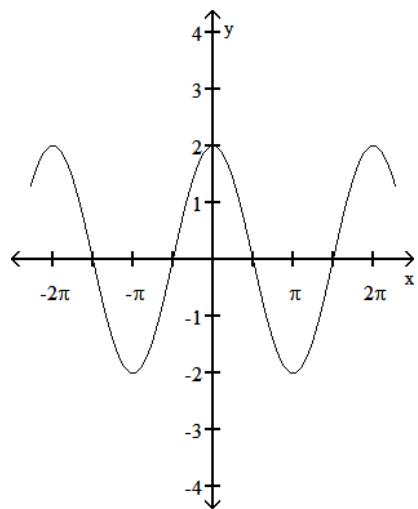


13) $y = 2 \cos x$

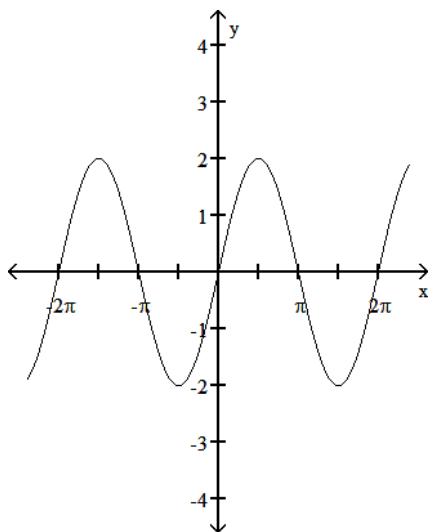
A)



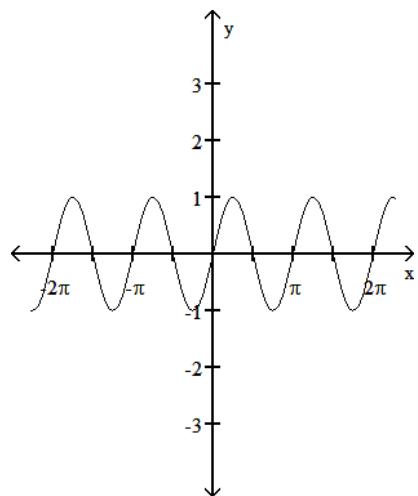
B)



C)



D)

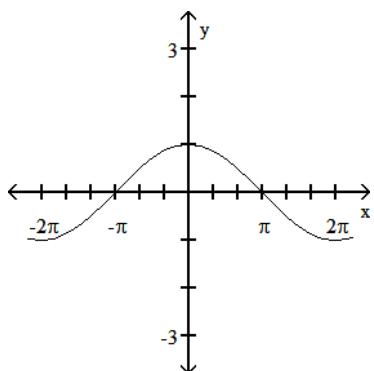


13) _____

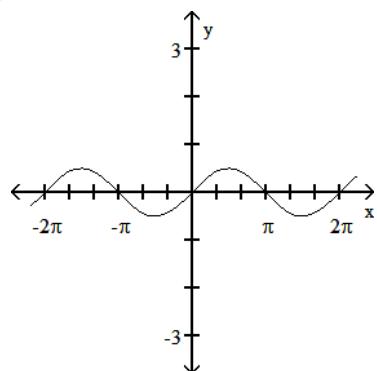
14) $y = \frac{1}{2} \cos x$

14) _____

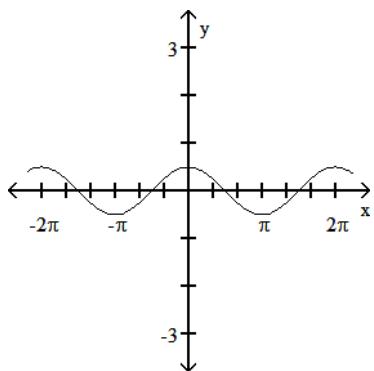
A)



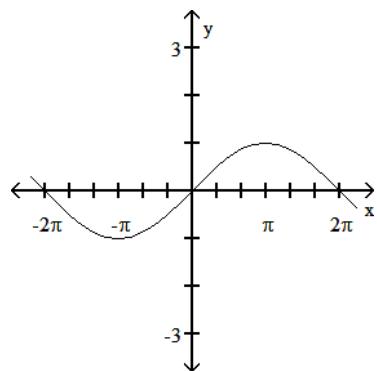
B)



C)



D)

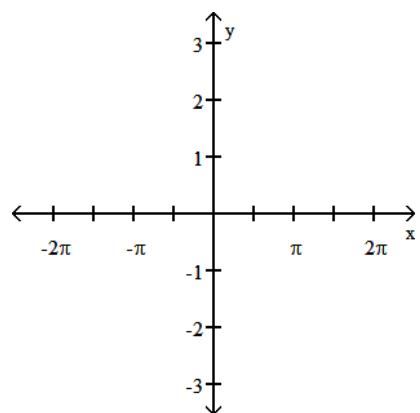


SHORT ANSWER.

Graph the function using key points.

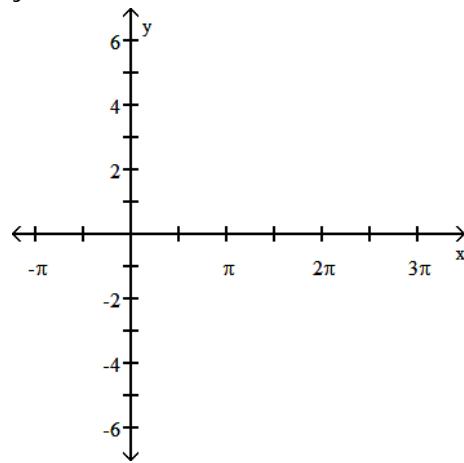
15) $y = \sin x - 2$

15) _____



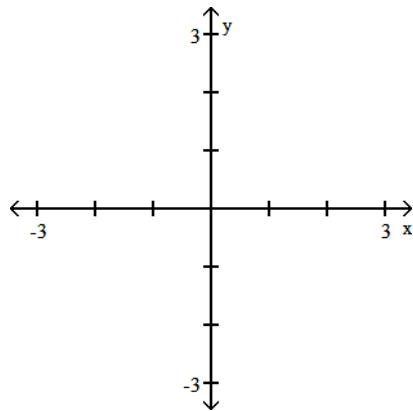
Graph the function.

16) $y = 2 \sin x$



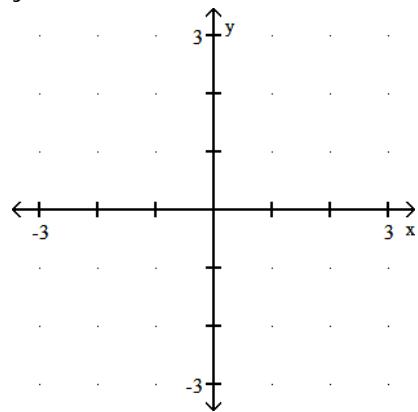
16) _____

17) $y = -3 \cos x$



17) _____

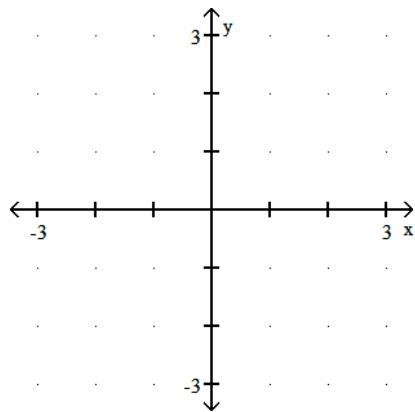
18) $y = -2 \sin x$



18) _____

19) $y = 0.4 \cos x$

19) _____

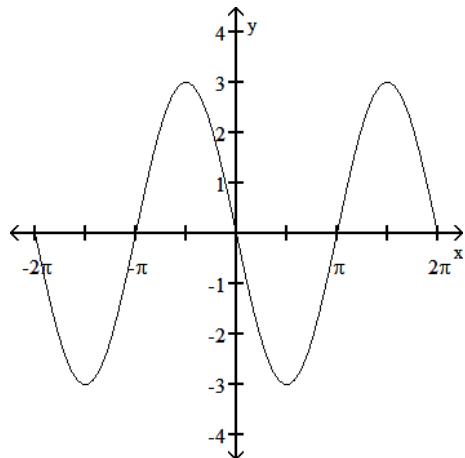


MULTIPLE CHOICE.

Find an equation in the form $y = A\cos x$ or $y = A\sin x$ that represents the given graph.

20)

20) _____



A) $y = 3\cos x$

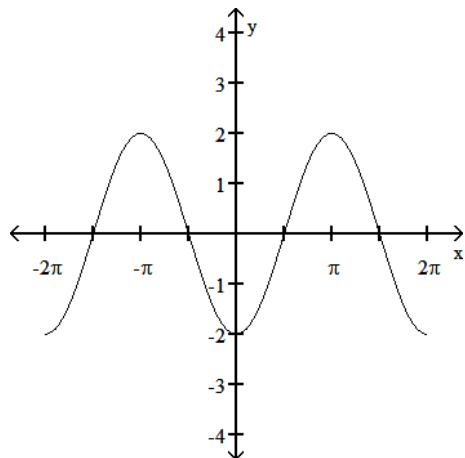
B) $y = -3\cos x$

C) $y = -3\sin x$

D) $y = 3\sin x$

21)

21) _____



A) $y = 2\cos x$

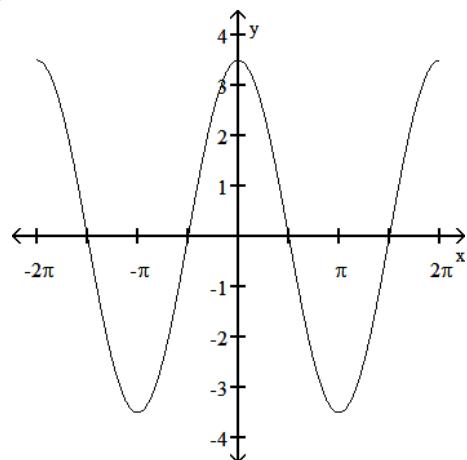
B) $y = -2\cos x$

C) $y = -2\sin x$

D) $y = 2\sin x$

22)

22) _____



A) $y = 3.5\cos x$

B) $y = -3.5\cos x$

C) $y = 3.5\sin x$

D) $y = -3.5\sin x$

Answer Key

Testname: MATH 06 - TRIG SECTION 7

1) B

2) C

3) $\frac{\pi}{2}, \frac{3\pi}{2}$

4) $\frac{3\pi}{2}$

5) $\frac{3\pi}{4}, \frac{7\pi}{4}$

6) $\frac{\pi}{6}, \frac{11\pi}{6}$

7) $\frac{5\pi}{4}, \frac{7\pi}{4}$

8) $\frac{\pi}{6}, \frac{5\pi}{6}$

9) 0

10) C

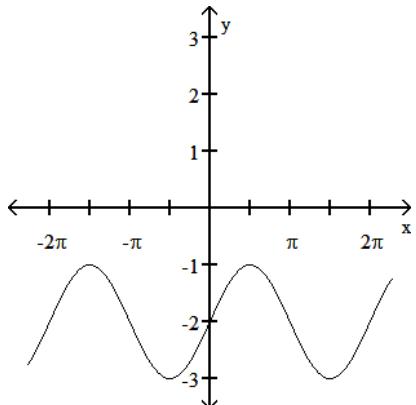
11) B

12) A

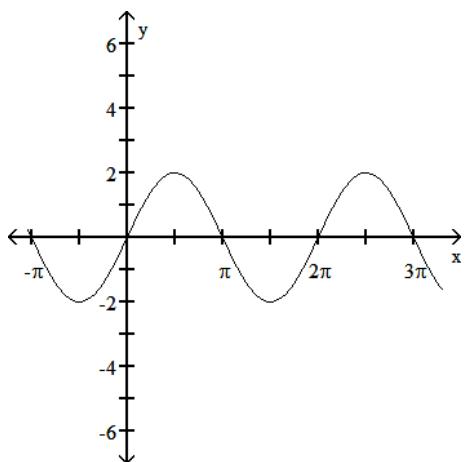
13) B

14) C

15)



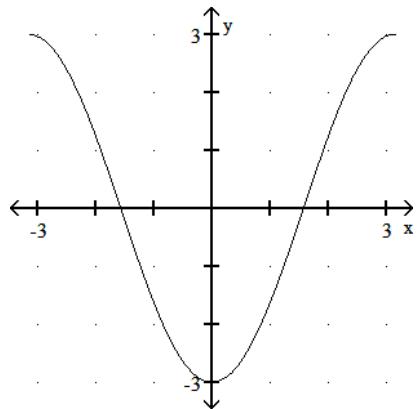
16)



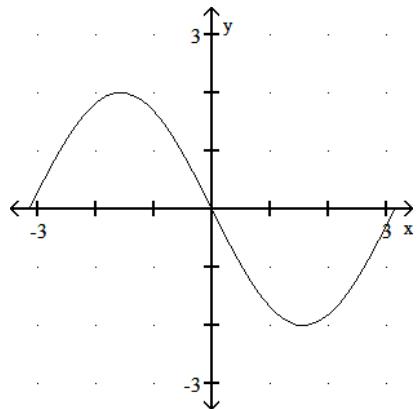
Answer Key

Testname: MATH 06 - TRIG SECTION 7

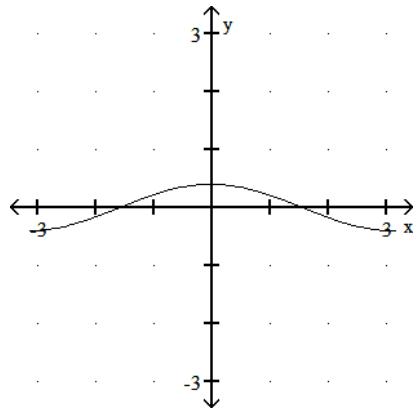
17)



18)



19)



20) C

21) B

22) A

Trig Section 3.1: Trigonometric Identities

MULTIPLE CHOICE.

Use the fundamental identities and appropriate algebraic operations to simplify the expression.

1) $\cos x (\csc x - \sec x) - \cot x$ 1) _____
A) -1 B) 1 C) 0 D) $\cos^2 x - \tan^2 x$

2) $\sin^2 x (\cot^2 x + 1)$ 2) _____
A) 1 B) $\cos^2 x + 1$ C) $\tan^2 x$ D) -1

3) $\frac{\cos x}{1 + \sin x} + \tan x$ 3) _____
A) 1 B) $\cos x + \sin x$ C) $\sin^2 x$ D) $\sec x$

4) $\frac{1 + \tan^2 x}{\sec x}$ 4) _____
A) $\csc x$ B) $\sec x$ C) - $\sec x$ D) 1

5) $\frac{\cos^2 x}{\sin^2 x} + \cos x \sec x$ 5) _____
A) $\csc x$ B) $\cot^2 x$ C) $\csc^2 x$ D) $\sec^2 x$

6) $1 - \frac{\cos^2 x}{1 + \sin x}$ 6) _____
A) 0 B) $\cot x$ C) $\sin x$ D) $\tan x$

SHORT ANSWER.

Verify the identity.

7) $\tan x (\csc x - \sin x) = \cos x$ 7) _____

8) $(1 - \cos x)(1 + \cos x) = \sin^2 x$ 8) _____

9) $(\sec x - \tan x)(\sec x + \tan x) = 1$ 9) _____

10) $(1 + \tan^2 x)(1 - \sin^2 x) = 1$ 10) _____

11) $\frac{\sec x - 1}{\tan x} = \frac{\tan x}{\sec x + 1}$ 11) _____

12) $1 + \sec^2 x \sin^2 x = \sec^2 x$ 12) _____

Answer Key

Testname: MATH 06 - TRIG SECTION 8

- 1) A
- 2) A
- 3) D
- 4) B
- 5) C
- 6) C

$$7) \tan x(\csc x - \sin x) = \tan x \cdot \csc x - \tan x \cdot \sin x = \frac{\sin x}{\cos x} \cdot \frac{1}{\sin x} - \frac{\sin x}{\cos x} \cdot \sin x = \frac{1}{\cos x} - \frac{\sin^2 x}{\cos x} = \frac{1 - \sin^2 x}{\cos x} = \frac{\cos^2 x}{\cos x} = \cos x$$

$$8) (1 - \cos x)(1 + \cos x) = 1 - \cos^2 x = \sin^2 x$$

$$9) (\sec x - \tan x)(\sec x + \tan x) = \sec^2 x - \tan^2 x = 1$$

$$10) (1 + \tan^2 x)(1 - \sin^2 x) = \sec^2 x \cdot \cos^2 x = \frac{1}{\cos^2 x} \cdot \cos^2 x = 1$$

$$11) \frac{\sec x - 1}{\tan x} = \frac{\sec x - 1}{\tan x} \cdot \frac{\sec x + 1}{\sec x + 1} = \frac{\sec^2 x - 1}{\tan x(\sec x + 1)} = \frac{\tan^2 x}{\tan x(\sec x + 1)} = \frac{\tan x}{\sec x + 1}$$

$$12) 1 + \sec^2 x \sin^2 x = 1 + \frac{\sin^2 x}{\cos^2 x} = 1 + \tan^2 x = \sec^2 x.$$